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Dear Dr.Arias, BIPM,

Attached is the first report on the frequency measurement by NMIJ-F1, a cesium atomic fountain frequency standard of NMIJ. Two measurements are reported and their measurement periods were ten days each. The measurement dates are **MJD 53549-53559** and **MJD 53589-53599**. The details of the uncertainty evaluation are described in the report.

Sincerely yours,

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Frequency comparison between H-Maser(405014) and Cs Fountain (NMIJ-F1) during **MJD 53549-53559** and **MJD 53589-53599**

National Metrology Institute of Japan(NMIJ) has measured the frequency of our Hydrogen maser HM (Clock # 405014) using the Cs atomic fountain frequency standard NMIJ-F1 during **MJD 53549-53559** and during **MJD 53589-53599**. The results are shown in Tables 1 and 2. Uncertainties are larger than the preliminary estimations Ref. [1, 2], because the present operational conditions are slightly different from those days. The conditions will be improved, and will approach to the best one in future.

<b>Period</b>	<b>53549-53559</b>
Measurement ratio	98.3 %
Y(NMIJ-F1)-Y(Maser 405014)	37.1
$u_A$	1.1
$u_B$	3.8
$u_{link / lab}$	0.5

Table 1. Results of the comparison in  $1 \times 10^{-15}$  unit.

<b>Period</b>	<b>53589-53599</b>
Measurement ratio	93.5 %
Y(NMIJ-F1)-Y(Maser 405014)	100.2
$u_A$	1.1
$u_B$	4.0
$u_{link / lab}$	0.5

Table 2. Results of the comparison in  $1 \times 10^{-15}$  unit.

The uncertainty budgets of NMIJ-F1 in the two measurements are shown in Tables 3 and 4. The estimation procedures are described in Ref [1-4].

Source of uncertainty	Bias	Uncertainty
2 <sup>nd</sup> order Zeeman	185.2	0.7
Blackbody radiation	-18.0	1.4
Gravitation	1.6	0.1
Cold collisions	0.0	3.3
Distributed cavity phase	-	1.2
Total	168.8	3.8

Table 3. Frequency biases and uncertainties in NMIJ-F1 during the period **MJD 53549-53559** in  $1 \times 10^{-15}$  unit.

Source of uncertainty	Bias	Uncertainty
2 <sup>nd</sup> order Zeeman	181.7	2.0
Blackbody radiation	-17.2	0.9
Gravitation	1.6	0.1
Cold collisions	0.0	3.3
Distributed cavity phase	-	1.2
Total	166.1	4.0

Table 4. Frequency biases and uncertainties in NMIJ-F1 during the period **MJD 53589-53599** in  $1 \times 10^{-15}$  unit.

The uncertainties  $u_A$ ,  $u_{link/lab}$ ,  $u_B$  are described in the following briefly.

1. Type A uncertainty  $u_A$

The NMIJ-F1 uses an optical molasses to load the atoms, and its frequency stability,  $\sigma_y(\tau)$ , is about  $1 \times 10^{-12} \tau^{-1/2}$ . Assuming white FM noise over the comparison period, the measurement uncertainty based on the frequency instability is  $1.1 \times 10^{-15}$  for 10 days.

2. Uncertainty of the link in the laboratory  $u_{link/lab}$

The uncertainty of the link in the laboratory,  $u_{link/lab}$ , consists of two factors as written in the following equation,

$$u_{link/lab} = \sqrt{u_{dead\ time}^2 + u_{link/maser}^2}, \quad (1)$$

where  $u_{link/maser}$  is the uncertainty due to the noise of the phase comparator between the fountain and HM,  $u_{dead\ time}$  is the uncertainty due to the operational dead time of the fountain. NMIJ-F1 was operated almost continuously and its efficiencies were 98.3 % during **MJD 53549-53559** and 93.5 % during **MJD 53589-53599** respectively. The operation was only interrupted sometimes due to earthquakes, electric power failures and so on, and  $u_{dead\ time}$  in the two measurements were  $1 \times 10^{-16}$  during **MJD 53549-53559**, and  $2 \times 10^{-16}$  during **MJD 53589-53599** respectively. The resulting uncertainty contributing to  $u_{link/lab}$  is shown in Tables 5 and 6.

	Uncertainty
$u_{link/maser}$	0.5
$u_{dead\ time}$	0.1

Table 5. Uncertainty is expressed in  $1 \times 10^{-15}$  unit during **MJD 53549-53559**

	Uncertainty
$u_{link/maser}$	0.5
$u_{dead\ time}$	0.2

Table 6. Uncertainty is expressed in  $1 \times 10^{-15}$  unit during **MJD 53589-53599**

### 3. Type B uncertainty $u_B$

#### A. 2<sup>nd</sup> order Zeeman shift

Using the linear Zeeman shift of the  $|F=3, m=-1\rangle \rightarrow |F=4, m=-1\rangle$  transition, frequency bias induced by the quadratic Zeeman shift of the clock transition is estimated from the following equation,

$$\Delta\nu_{quadratic\_Zeeman} = \frac{8(\delta\nu_{linear\_Zeeman})^2}{\nu_0}, \quad (2)$$

where  $\Delta\nu_{quadratic\_Zeeman}$  is the relative frequency shift, and  $\nu_0$  is the resonance frequency of clock transition. The details of the approach to estimate uncertainty of the quadratic Zeeman shift is described in Ref. [3]

#### B. Black body radiation

The temperature of the drift region was estimated from the measurement with a platinum thermometer attached to the vacuum chamber and the measurement of the resonance frequency on the microwave cavity that has a temperature coefficient of 150 kHz/°C. The black body radiation shift is estimated using the following equation.

$$\Delta\nu_{BBR} = -1.711 \times 10^{-14} \times \left(\frac{T}{300}\right)^4 \left[1 + 0.014 \times \left(\frac{T}{300}\right)^2\right] \quad (3)$$

The frequency biases and uncertainties due to the black body radiation in the two measurements (**MJD 53549-53559** and **MJD 53549-53559**) were different, because we slightly changed the temperature of the vacuum chamber.

#### C. Gravitational red shift

The microwave cavity is located at a height of  $14.3 \pm 0.5$  m above sea level. The gravitational red shift is estimated using the following equation.

$$\Delta\nu_{RS} = 1.09 \times 10^{-16} \times h \quad (4)$$

#### D. Cold collisions

NMIJ-F1 was operated using a low density optical molasses for the present measurements. In the optical molasses configuration, a smaller collisional frequency shift is expected than that in the MOT configuration that was used for the estimation of

the collisional frequency shift of  $(2.7 \pm 0.6) \times 10^{-15}$  [2]. We consider the value of  $3.3 \times 10^{-15} = (2.7 + 0.6) \times 10^{-15}$  as the uncertainty for the moment, and 0 as the frequency bias. Actually, we operated in different number of atoms with the molasses configuration, but a significant frequency change depending on the number of atoms was not observed. The resolution of its observation is currently limited by the frequency stability of NMIJ-F1, then we need longer accumulation time to estimate the collisional frequency shift more precisely. That is remained as our future subject.

#### F. Distributed cavity phase

The microwave cavity used in NMIJ-F1 has two ports to couple with the oscillated magnetic field from a local oscillator. Presently a single port is used to introduce the oscillated magnetic field. In this configuration, the uncertainty due to the distributed cavity phase shift is estimated to be  $1.2 \times 10^{-15}$ . The method to determine this uncertainty is described in Ref. [4].

#### References

- [1] Takayuki Kurosu, Yasuhiro Fukuyama, Yasuki Koga and Kentaro Abe, "Preliminary evaluation of the Cs atomic fountain frequency standard at NMIJ/AIST." IEEE Trans. Instrum. Meas., vol. 53, pp. 466-471, 2004
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- [3] Takayuki Kurosu, Yasuhiro Fukuyama, Kentaro Abe and Yasuki Koga, "Measurement of a Weak magnetic field using cold atoms." Jpn. J. Appl. Phys. 41, pp. L586-588, 2002.
- [4] S. Yanagimachi, Y. Fukuyama, T. Ikegami and T. Kurosu, "Numerical Simulation of Distributed Cavity Phase Shift in Atomic Fountain Standard." Jpn. J. Appl. Phys. 44, pp. 1468-1475, 2005.