# Evaluation of PTB primary caesium fountain frequency standard CSF1 between MJD 59334 - MJD 59364

PTB's primary caesium fountain frequency standard CSF1 was operated between MJD 59334, 0:00 UTC and MJD 59364, 0:00 UTC. Frequency comparisons were made with respect to PTB hydrogen maser H9, BIPM code 1400509.

The relative frequency instability of the relative frequency differences y(CSF1-H9) was  $10.5\times10^{-14}\cdot(\tau/s)^{-1/2}$  during the 30 days. The actual measurement time amounts to 95.4% of the 30 × 24 hours. This results in a statistical uncertainty  $u_A = 0.07\times10^{-15}$ , assuming that white frequency noise is the dominant noise source.

For the statistical uncertainty due to the clock link  $u_{A/Lab} = 0.02 \times 10^{-15}$  is obtained by taking into account the actual measurement time, while the systematic uncertainty due to the clock link  $u_{B/Lab}$  is negligible. Finally, the estimated uncertainty for the link to TAI for 30 days is  $u_{TAI} = 0.07 \times 10^{-15}$ .

Frequency corrections for the following effects were applied to the raw data:

- Zeeman effect (magnetic field along the atoms' trajectory)
- black body effect (thermal radiation along the atoms' trajectory)
- relativistic redshift and relativistic Doppler effect
- cold collisions effect
- distributed cavity phase effect
- microwave lensing effect

The CSF1 standard uncertainty  $u_B$  is estimated as  $2.8 \times 10^{-16}$  (1  $\sigma$ ) for the relevant period [1].

### Table of results of CSF1 compared to hydrogen maser H9 (1400509)

Interval of evaluation MJD 59334, 0:00 UTC – MJD 59364, 0:00 UTC

Fractional dead time 4.6%

Resulting frequency difference  $y(CSF1 - H9) = 22.85 \times 10^{-15}$ 

Type A uncertainty  $u_A$  (1  $\sigma$ ) 0.07 × 10<sup>-15</sup>

Type B uncertainty  $u_B$  (1  $\sigma$ ) 0.28  $\times$  10<sup>-15</sup>

Link to clock  $u_{A/Lab}$  (1  $\sigma$ )  $0.02 \times 10^{-15}$ 

Link to clock  $u_{\rm B/Lab}$  (1  $\sigma$ )  $0.00 \times 10^{-15}$ 

Link to TAI  $u_{TAI}$  (1  $\sigma$ ) 0.07 × 10<sup>-15</sup> (30 days)

Combined uncertainty (1  $\sigma$ ) 0.30  $\times$  10<sup>-15</sup>

#### Type A (statistical) uncertainty of CSF1

For the microwave synthesis the previously utilized optically stabilized microwave oscillator [2] has been replaced by a new system for the optical generation of ultrastable microwave signals. The new system utilizes the same cavity stabilized laser as before, but a new commercial frequency comb system, where the microwave signal is obtained from a photodiode. As before this signal is locked to a hydrogen maser in the long-term and employed as local oscillator for the PTB fountain clocks.

The frequency instability  $10.5 \times 10^{-14} (\tau/s)^{-1/2}$  of the measured relative frequency differences y(CSF1 – Hmaser) is obtained for the combination of low and high density operation and gives the statistical measurement uncertainty  $u_A$  [1].

The optically stabilized microwave system was available during >97% of the TAI measurement interval. Alternatively a quartz-based frequency synthesis system was employed.

#### Type B (systematic) uncertainty of CSF1

In the table below we report the type B uncertainty evaluation results valid for the evaluation at hand. Detailed descriptions of the systematic uncertainty contributions of CSF1 have been published elsewhere [1].

At the 26<sup>th</sup> CGPM in November 2018, TAI has been newly defined (Resolution 2). As a result the relativistic redshift of a clock contributing to TAI is to be computed with respect to the conventionally adopted equipotential  $W_0 = 62\,636\,856.0\,\text{m}^2\text{s}^{-2}$  of the Earth's gravity potential. The differentiation relating to the uncertainty of the relativistic redshift for the case of TAI contributions of the PTB fountain clocks in [1] is therefore no longer needed, so that a relativistic redshift uncertainty of  $0.02 \times 10^{-16}$  [1] is attributed now and in the future.

## Frequency shifts, corrections and type B uncertainties of CSF1 (parts in 10<sup>16</sup>):

| Frequency shift                          | Correction | Uncertainty |
|--|------------|-------------|
| Quadratic Zeeman shift                   | - 1078.77  | 0.10        |
| Blackbody radiation shift                | 166.57     | 0.81        |
| Relativistic redshift and Doppler effect | - 85.56    | 0.02        |
| Collisional shift                        | -16.0      | 2.5         |
| Distributed cavity phase shift           | - 0.04     | 0.93        |
| Microwave lensing                        | -0.4       | 0.2         |
| AC Stark shift (light shift)             |            | 0.01        |
| Rabi and Ramsey pulling                  |            | 0.013       |
| Microwave leakage                        |            | 0.01        |
| Electronics                              |            | 0.1         |
| Background gas collisions                |            | 0.4         |
| Total type B uncertainty                 |            | 2.8         |

## References

[1] S. Weyers, V. Gerginov, M. Kazda, J. Rahm, B. Lipphardt, G. Dobrev and K. Gibble, Metrologia **55**, pp. 789–805 (2018), <a href="https://doi.org/10.1088/1681-7575/aae008">https://doi.org/10.1088/1681-7575/aae008</a>

[2] B. Lipphardt, V. Gerginov, S, Weyers, IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control **64**, pp. 761–766 (2017), <a href="https://ieeexplore.ieee.org/document/7807353">https://ieeexplore.ieee.org/document/7807353</a>