

Frequency evaluation of Maser 1401103 by IT-Yb1 for the period MJD 59384 to 59389

During the period MJD 59384 – 59389 (19 June 2021–24 June 2021) INRIM evaluated the frequency of the hydrogen maser IT-HM3 (BIPM code 1401103) using the Yb optical lattice frequency standard IT-Yb1 and an optical frequency comb. The evaluation is based on the CCTF2017 recommended frequency for 171 Yb as a secondary representation of the second, $f(^{171}$ Yb) = 518 295 836 590 863.6 Hz with a relative standard uncertainty of $u_{\rm Srep} = 5 \times 10^{-16}$ [1, 2]. The results of the evaluation are summarized in Tab. 1. Details of IT-Yb1 operation and uncertainty budget are given in Refs. [3, 4] and summarized below.

1 Frequency measurement

The clock laser of IT-Yb1 is stabilized on an ultrastable cavity and probes ¹⁷¹Yb atoms trapped in an optical lattice at the magic frequency. A digital control loop acting on an acousto-optic modulator keeps the clock laser frequency in resonance with the atoms. The cavity-stabilized laser is sent to a fibre frequency comb referenced to IT-HM3. The frequency ratio between the ¹⁷¹Yb transition and IT-HM3 is calculated from the comb measurements and the corrections used for steering the acousto-optic modulator.

Table 1: Final evaluation using IT-Yb1.

| Period of estimation | y(HM1401103 /ITYb1) | u_{A} | u_{B} | $u_{\mathrm{A/lab}}$ | $u_{\rm B/lab}$ | u_{Srep} | Uptime |
|----------------------|------------------------|------------------|------------------|----------------------|-----------------|---------------------|--------|
| UIIIauIOII | $/10^{-16}$ | $/10^{-16}$ | $/10^{-16}$ | $/10^{-16}$ | $/10^{-16}$ | $/10^{-16}$ | |
| 59384-59389 | 134.0 | 0.1 | 0.3 | 3.7 | 0.2 | 5 | 14% |

Table 2: Uncertainty budget for IT-Yb1 for the reported period.

| Effect | Rel. Shift/ 10^{-17} | Rel. Unc./ 10^{-17} |
|----------------------------------|------------------------|-----------------------|
| Density shift | -0.6 | 0.5 |
| Lattice shift | 3.4 | 1.5 |
| Zeeman shift | -3.13 | 0.03 |
| Blackbody radiation shift (room) | -234.8 | 1.3 |
| Blackbody radiation shift (oven) | -1.2 | 0.6 |
| Static Stark shift | -23 | 2 |
| Probe light shift | 0.04 | 0.03 |
| Background gas shift | -0.5 | 0.2 |
| Servo error | 0.0 | 0.3 |
| Other shifts | 0.0 | 0.1 |
| Grav. redshift (static) | 2599.5 | 0.3 |
| Grav. redshift (tides) | 0 | 2 |
| Total | 2339.9 | 3.5 |

2 IT-Yb1 evaluation

The uncertainty $u_{\rm A}$ is the statistical contribution from the instability of IT-Yb1. The uncertainty $u_{\rm B}$ is the systematic uncertainty of IT-Yb1 [4]. The systematic frequency shift and uncertainty budget of IT-Yb1 for the reported period are given in Tab. 2. IT-Yb1 now operates with a vertical optical lattice and the lattice light shift calculations have been updated following Ref. [5]. The table includes the gravitational redshift relative to the conventional potential $W_0 = 62\,636\,856.0\,{\rm m}^2{\rm s}^{-2}$ [4]. Given the short operation of the clock we added a contribution to the gravitational redshift uncertainty coming from tides.

3 Link evaluation

The uncertainty $u_{\rm l/lab}$ is due to the link between IT-Yb1 and IT-HM3, including the optical to microwave comparison at the comb. Table 3 summarizes the contributions to this uncertainty.

The comparison uncertainty between optical and microwave signals at the comb has been evaluated from comparison with a second optical frequency comb.

IT-Yb1 and the comb were operated for 59 184 s (uptime 14% of the evaluation period). The data collected and the distribution of the uptimes of IT-Yb1 are shown in Fig. 1. Extrapolation using the maser as a flywheel is needed given the intermittent operation of IT-Yb1. Its evaluation is separated in an uncertainty from dead times and a correction for the maser drift. The maser drift of $-5.9(2) \times 10^{-16}$ /d has been calculated from IT-Yb1 data collected between MJD 59384 and 59464. The contribution from dead times has been evaluated following the approach in Ref. [6]. For this measurement we

Table 3: Uncertainty budget for the link between IT-Yb1 and IT-HM3 for the reported period.

| Effect | Uncertainty/ 10^{-16} |
|----------------------------------|-------------------------|
| Comb statistic | 0.3 |
| Extrapolation (dead time) | 3.7 |
| Extrapolation (drift) | 0.3 |
| Total $u_{\rm A/lab}$ | 3.7 |
| Optical/microwave comp. (type B) | 0.2 |
| Total $u_{\rm B/lab}$ | 0.2 |

considered the IT-HM3 noise to be a power-law model described by the Allan deviation: white phase noise $3 \times 10^{-13} (\tau/s)^{-1}$; white frequency noise $4 \times 10^{-14} (\tau/s)^{-1/2}$; flicker frequency noise 3×10^{-16} ; random walk frequency noise $2 \times 10^{-19} (\tau/s)^{1/2}$.

Contributors

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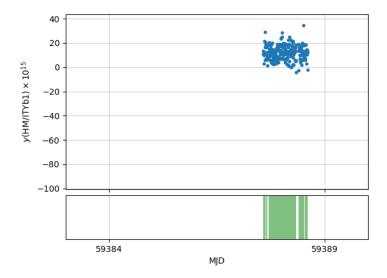


Figure 1: Fractional frequency deviation $y({\rm HM1401103/ITYb1})$ measured in the period MJD 59384 - 59389. Green shaded regions in the bottom plot represent the uptime of IT-Yb1.

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