How Primary and Secondary Frequency Standards contribute to international time scale performances

METP

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Summary

- The calculation of UTC, TT(BIPM), UTCr
 - Time links, clocks and algorithms
- TT(BIPM) algorithm will be introduced, and the latest calculation (2022) presented.
- The role of Primary and Secondary Frequency Standards (PSFS) in international time scale calculation, focusing on how they guarantee the long-term stability and accuracy of UTC.

The role of the BIPM

- The BIPM is the international organization responsible for:
 - the calculation and the publication of the Coordinated Universal Time (UTC)
 - its rapid solution, UTCr
 - the realization of Terrestrial Time TT(BIPM).
- UTC is calculated each month
- UTCr each week
- TT(BIPM) each year (each month for internal use)

All the results are published in the BIPM website <u>https://www.bipm.org/en/time-metrology</u>

UTC, UTCr and TT(BIPM)



Geographical distribution of the laboratories that contribute to TAI and time transfer equipment (2023)



Atomic clocks in UTC



NTSC Rubidium Fountain











Hydrogen Masers

2023.5

Clocks in different laboratories are compared by suitable time and frequency transfer techniques

Global Navigation Satellite Systems (GNSS)

GNSS are based on time broadcasting from satellites to ground receivers (one-way time transfer). Distant labs equipped with GNSS receivers periodically compare their clocks to the broadcasted time and send the result to the BIPM. Typical algorithms are All in View, Common View, and Precise Point Positioning



Progress in GNSS measures

GPS+ GLONASS + Beidou + Galileo IPPP : Precise Point Positioning with integer ambiguity resolution

Two-Way Satellite Time & Freq. Transfer (TWSTFT)

dedicated ground terminals simultaneously receive and transmit time transfer signals (two-way time transfer) on geostationary telecom satellites. Two-way method cancels out (at first order) the propagation time of the signal.



Progress in TWSTFT Software Designed Radio and TWSTFT Carrier Phase

In development : Optical Fiber links

A growing number of UTC laboratories are gaining access to fiber links dedicated to time and frequency. Although few of them are currently interconnected by operational, highduty cycle links, this number is expected to grow quickly during the next decade.



UTC, UTC(k) and [UTC-UTC(k)]

- UTC Stability based on the **atomic clocks** (420) (and PSFS) Steering procedure based on PSFS availability
- UTC(k) Stability based on the **laboratory equipment** Steering procedure to be close to UTC
- [UTC-UTC(k)] UTC, UTC(k) and time links used to compare clocks



Difference between UTC and UTC(k)



• UTC a time scale optimized to be stable in frequency at very long term. EAL provides the stability

• UTC unit is the SI second

- UTC is steered in **FREQUENCY** to be close to the frequency of PFSF (d published monthly in CirT)
- UTC(k) is generally steered in **FREQUENCY** and in **TIME** to be close to UTC

Primary and Secondary standards contributing to UTC



Graphical representation of all evaluations of Primary and Secondary Frequency Standards reported since Circular T 190. Enhanced color dots indicate evaluations carried out within the month of TAI computation.

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https://webtai.bipm.org/database/show_psfs.html

The role of PSFS in UTC

- In this presentation I'll highlight the role of PSFS in ensuring the logterm stability of UTC and its accuracy.
- It will be discussed:
 - the algorithm used to evaluate EAL (prediction and weight) (stability).
 - the algorithm to calculate TT(BIPM).
 - the algorithm to evaluate the difference between TAI and PSFS (accuracy).

First step: EAL - 1



N is the number of atomic clocks *w_i* the relative weight of the clock *H_i*. *h_i(t)* is the reading of clock *H_i* at time *t h_i'(t)* is the prediction of the reading of clock *H_i*

The weights of the clocks obey the relation:

$$\sum_{i=1}^{N} w_i = 1$$

First step: EAL - 2

The system solved by the algorithm:

$$\begin{cases} \sum_{i=1}^{N} w_i x_i(t) = \sum_{i=1}^{N} w_i h'_i(t) \\ x_i(t) - x_j(t) = x_{i,j}(t) \end{cases}$$

where

$$x_i(t) = EAL(t) - h_i(t)$$

The solution is:



The main algorithms used are:

- the **prediction algorithm** (quadratic model) - the weighting algorithm (each clock is weighted wrt to their stability/predictability)

The prediction algorithm

- The prediction algorithm has the scope to avoid/minimize any time and frequency steps to UTC when a clock is added or eliminated from the ensemble.
- Any deterministic signatures (x₀, y₀ and frequency drift) are estimated and eliminated by the clocks to avoid affecting UTC.



The estimation of the frequency drift

- It is a key issue for using at the best the hydrogen masers
- The reference used to estimate the frequency drift is the most important point; EAL and TAI are not enough stable to estimate the drift.
- The BIPM realization of TT, called TT(BIPM) is used to evaluate monthly the frequency drift of the hydrogen masers.
- The main components of TT(BIPM) are EAL and the PSFS.

- EAL is currently free from frequency drifts affecting H-Masers even if they are contributing with a global weight of 90%.
- This result is obtained because of the availability of PSFS allowing us to generate TT(BIPM) each month.
- We can conclude, as some extent, that PSFS allow to the BIPM:
 - To use at the best the Hydrogen Masers
 - To ensure a long-term stability to EAL

TT(BIPM)

- As TAI is computed in real time and never corrected in retrospect, it is not optimal. Therefore, the BIPM computes a post-processed time scale TT(BIPM).
- Each new version TT(BIPM) updates and replaces the previous one.
- TT(BIPM) calculation
 - Post-processed using all available PFS data, as of year 20xx.
 - f(EAL) is estimated each month using available PFS. Monthly estimates are smoothed and integrated to obtain TT(BIPMxx).
 - Last realization: TT(BIPM22), released in March 2023.

Algorithm used for estimating f(EAL)

 We want to estimate the frequency of EAL, over an estimation interval T from N PFS evaluations,

$$y = \sum_{j=1}^{N} a_j W_j$$

where:

- W_i is the rate difference between EAL and a PFS on a given interval T_i
- The filter coefficients a_i, are normalized and depend on
 - The uncertainty of the evaluation j. It is fully characterized by its components u_A, u_B. u_A is the combined uncertainty from that originated in the instability of the PFS, that of the link between the PFS and the clock participating to TAI (dead time included), and that of the link to EAL. u_B is the combined uncertainty from systematic effects
 - The distance between T_i and T
 - The instability of EAL, which transfers the evaluation from T_i to T

Uncertainty of f(TT(BIPM2022))

- We consider TT(BIPM) our best frequency reference to evaluate the performance of EAL, TAI and all the primary and secondary standards. Frequency accuracy improves with the standards:
 - < 1x10-15 since 2007</p>
 - < 0.5x10-15 since 2009</p>
 - $\le 0.3 \times 10^{-15}$ since 2012
 - $\leq 0.15 \times 10^{-15}$ since 2020



Uncertainty of f(TT(BIPM22))

Frequency standards reported for TAI over 10 years

Primary and secondary standards reported to the BIPM

- 2011 to 2016: 50-60 reports by ~10 fountains
- 2017/2018: 54/84 reports by 8/10 fountains + 2 optical lattices
- 2020: 114 reports by 11 Cs fountains+12 by SYRTE-FORb + 13 by 2 optical lattices
- 2021: 92 reports by 11 Cs fountains + 11 by SYRTE-FORb + 22 by 5 optical lattices
- 2022: 109 reports by 12 Cs fountains+10 by SYRTE-FORb + 50 by 6 optical lattices

EAL and TAI wrt TT(BIPM2022)

By using TT(BIPM) we can estimate the long-term stability of EAL.



If the short term of the Allan Variance is not useful because EAL and TT are strictly correlated at the short term, we can evaluate the long-term performances of EAL by analyzing it.

SYRTE - PSF/SFS wrt TT(BIPM)



Other results



2020

Years

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Comparison of primary and secondary frequency standards used for TAI

 Two studies (2012 and 2022) have been conducted in collaboration with G. Petit to analyze the level of agreement between the PSFSs compared with their stated uncertainty using TT(BIPM).



Graphical representation of all evaluations of Primary and Secondary Frequency Standards reported since Circular T 190. Enhanced color dots indicate evaluations carried out within the month of TAI computation.

Comparisons using TT(BIPM)

- 1. Study each PFS/SFS by comparison to TT(BIPM)
 - Estimate one frequency bias Y_i = <y(PSFS_i -TT(BIPM))> for each PSFS_i, weighting each evaluation y(PSFS_i -TT(BIPM)) using either the total uncertainty u
 - Estimate goodness of fit for each PSFS_i (Reduced Chi square χ^2 , Birge ratio R_{Bi})
- 2. Study the ensemble of PSFS:
 - Estimate if the distribution of frequency biases Y_i is consistent with the uncertainties u_{Bi} => Birge ratio of the series of frequency biases

Evaluation of PSFS performance: detailed formulas

From the series $y_i = y(PFS(t_i) - TT(BIPM))$, estimate one frequency bias

$$- \overline{Y} = \frac{\sum_{i=1}^{n} w_i y_i}{\sum_{i=1}^{n} w_i} \text{ where } w_i \text{ is } 1/u_i^2$$

Test the consistency of values y_i and uncertainties: Birge ratio $R_B = \sqrt{\frac{\sum_{i=1}^{n} \frac{(y_i - \overline{Y})^2}{u_i^2}}{(n-1)}}$

- $R_{\rm B}$: with the total uncertainty including
 - $-\ u_A$ originating in the instability of the PFS
 - u_{l/lab} uncertainty in the link between the PFS and the TAI clock
 - $\,u_{l/TAI}$ is the uncertainty in the link to TAI
 - u_B is the combined uncertainty from systematic effects
- $-R_{\rm B} > 1 \equiv$ uncertainties are underestimated
- $-R_{\rm B} < 1 \equiv$ uncertainties are overestimated or the measurements are correlated

Comparison of PFS to TT(BIPM) over 2006-2012

| Standard | $\overline{Y}/10^{-15}$ | $R_{\rm B}$ |
|-----------|-------------------------|-------------|
| IT-CSF1 | -0.25 | 1.60 |
| NICT-CSF1 | -0.93 | 0.93 |
| NIST-F1 | 0.25 | 1.43 |
| NPL-CSF2 | -0.24 | 1.28 |
| PTB-CSF1 | 0.82 | 1.10 |
| PTB-CSF2 | 0.38 | 1.22 |
| SYRTE-FO1 | -0.64 | 1.01 |
| SYRTE-FO2 | 0.13 | 1.27 |
| SYRTE-FOM | -0.37 | 0.87 |



PFS vs TT(BIPM) over 2016-2022

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Global improvement by a factor 3, reflected in the TT(BIPM) uncertainty Peak-to peak of fountain mean offset Y_i to TT is 3x10⁻¹⁶ vs. 1.8x10⁻¹⁵ 10 years ago

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Accuracy of UTC – Calculation of *d*

- Several laboratories in the world contribute to the accuracy of UTC providing the evaluations of PSFS to the BIPM.
- In Sec. 3 of Circular T:
 - The PSFS are evaluated singularly with respect to TAI
 - The algorithm used to calculate the Terrestrial Time (TT) is used to evaluate the frequency deviation of TAI (d = -y(TAI)) with respect to the ensemble of PSFS.



Section 3 of Circular T



If $|d| \ge 1 \times 10^{-15}$ a correction of about 0.2 x 10^{-15} is applied two months later.

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The frequency accuracy of TAI is estimated at the level of ~10⁻¹⁶

d values



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https://webtai.bipm.org/database/d_plot.html

UTCr – the rapid realization of UTC

Since 2013 a rapid evaluation of UTC is available, UTCr.

The data are on daily batches and published each week, the Wednesday.

The number of participating laboratories is slightly increased in the last years.

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|------------|---|---|------------------------------------|-----------------------------------|-----------------------------------|------------------------|------------------------|--------------|--|--|
| | Computed values of [UTCr-UTC(k)] | | | | | | | | | |
| ate | 2023 Øh UTC | SEP 4 | SEP 5 | SEP 6 | SEP 7 | SEP 8 | SEP 9 | SEP 10 | | |
| | MJD | 60191 | 60192 | 60193 | 60194 | 60195 | 60196 | 60197 | | |
| .abor | ratory k | tory k [UTCr-UTC(k)]/ns | | | | | | | | |
| 105 | (Borowiec) | -3.3 | -3.2 | -3.1 | -3.3 | -3.5 | -3.4 | -3.6 | | |
| NUS | (Sydney) | -446.2 | -447.5 | -444.2 | -441.5 | -436.8 | -438.5 | -438.6 | | |
| BEV | (Wien) | -16.0 | -17.6 | -19.5 | -22.6 | -27.6 | -30.4 | -30.6 | | |
| BIRM | (Beijing) | 1.6 | 2.4 | 3.5 | 5.3 | 4.6 | 5.6 | 6.5 | | |
| CH | (Bern-Wabern) | -1.1 | -1.3 | -1.4 | -1.6 | -1.5 | -1.5 | -1.9 | | |
| CNM | (Queretaro) | -4.8 | | | | | | | | |
| CNMP | (Panama) | -5.9 | 2.6 | 5.1 | 5.1 | 4.8 | 0.4 | 6.1 | | |
| DMDM | (Belgrade) | -7.6 | -16.4 | -17.9 | -22.5 | -24.7 | -28.9 | -32.0 | | |
| DTAG | (Frankfurt/M) | -26.2 | -27.0 | -25.2 | -25.3 | -26.4 | -27.6 | -28.6 | | |
| esa | (Noordwijk) | -0.2 | -0.1 | 0.0 | -0.1 | 0.2 | 0.4 | 0.0 | | |
| нко | (Hong Kong) | 547.2 | 549.8 | 550.4 | 551.9 | 555.4 | 554.5 | 556.2 | | |
| ICE | (San Jose) | -31.9 | -51.5 | -49.1 | -38.5 | -60.3 | -51.0 | -60.9 | | |
| IFAG | (Wettzell) | -780.2 | -782.3 | -780.3 | -780.7 | -779.0 | -778.5 | -776.2 | | |
| IGNA | (Buenos Aires) | -4292.4 | -4305.6 | -4326.8 | -4343.4 | -4355.2 | -4371.1 | -4382.7 | | |
| IMBH | (Sarajevo) | 0.4 | 0.4 | 0.4 | 0.0 | 0.2 | 0.3 | 0.3 | | |
| INTI | (Buenos Aires) | 275.0 | 279.5 | 279.7 | 279.2 | 268.3 | 270.6 | 274.2 | | |
| INXE | (Rio de Janeiro) | -12.7 | -13.2 | -8.8 | -5.9 | -1.7 | 1.3 | 5.6 | | |
| IPQ | (Caparica) | 923.5 | 924.8 | 925.1 | 929.9 | 930.8 | 931.3 | 935.9 | | |
| П | (lorino) | -0.1 | -0.5 | -1.0 | -1.3 | -1.5 | -1.5 | -1.7 | | |
| JV IV | (Kjeller) | 1.6 | 1.4 | 1.6 | 0.9 | 0.2 | 0.7 | 0.5 | | |
| CRIS | (Daejeon) | -2.8 | -2.9 | -2.8 | -2.5 | -2.3 | -2.5 | -2.7 | | |
| 2 | (Astana) | 1.4 | 1.3 | 1.2 | 0.9 | 0.0 | -1.0 | -1.1 | | |
| | (Sao Carlos) | 1.8 | 0.7 | 2.4 | 2.3 | 3.3 | 4.9 | 3.9 | | |
| UX | (Belvaux) | 0.5 | -3.2 | -4.4 | -2.7 | -5.7 | -5.4 | -4.8 | | |
| TASM | (Bayanzurkh) | -543.4 | -556.9 | -565.9 | -5/1.3 | -5/8.7 | -591.6 | -600.3 | | |
| TIKE | (Espoo) | 2.9 | 2.0 | 2.5 | 1.8 | 1.1 | 0./ | 0.4 | | |
| ISL | (Lower Hutt) | 83.6 | 8/.1 | 82.3 | 82.1 | 85.8 | 86.5 | 8/.6 | | |
| In C | (паккап) | -3770.0 | -3768.3 | -3//2.5 | -3775.3 | -3777.8 | -3782.0 | -3786.4 | | |
| VAU | (Mizusawa) | 451.2 | 452.4 | 456.7 | 461.1 | 465.5 | 467.2 | 469.1 | | |
| | | -1.6 | -1.3 | -1.6 | -1.4 | -1.6 | -1.5 | -1.5 | | |
| MTN | (Beijing) | -1./ | -1.9 | -1.9 | -1.8 | -2.5 | -2.1 | -1.5 | | |



UTCr versus UTC

For the week 2336 for example we had 62 participating laboratories with 260 atomic clocks.

Concerning the time links, we apply the following politics:

- if in UTC the combination of TW and GPS PPP is used in UTCr the TW
- If in UTC we use GPS PPP \implies in UTCr GPS P3



Stability of UTCr

- UTCr was not conceived to have a very good long-term stability (major difference from UTC) but to give access to UTC with a short latency to the participating laboratories.
- The goal for UTCr is to be as close as possible to UTC $(\pm 2 ns)$
- The algorithm used for the stability is like UTC algorithm
 - quadratic prediction
 - weight algorithm attributing to the clocks a weight based on the predictability/stability

Accuracy of UTCr

- The accuracy for UTCr means that UTCr must be as close as possible to UTC.
- No frequency steering is applied
- Steering in time is applied each month after the publication of Circular T.



Conclusions

- The contribution of PSFS to UTC is crucial to ensure:
 - The use of the clocks (hydrogen Masers) at the best of their capabilities
 - The constant improvement of long-term stability and accuracy of UTC
- The contribution to UTC of SFS is also a requirement for the possible redefinition of the second
- The BIPM thanks all the laboratories and the SYRTE in particular for their strong engagement in providing regularly PSFS data to the BIPM.

Thank you very much for your attention